## 429. Kinetics of the Thermal Decomposition of Acetals. Part II. ${ }^{1}$ The Methylal Chain.

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The kinetics of the thermal decomposition of methylal has been studied over the range $472-520^{\circ}$ and $50-450 \mathrm{~mm}$. in a static system, by studying the change of pressure and by infrared analyses. The system of steadystate equations is too complex to have a straightforward solution but by means of them the experimental order is explained, several stoicheiometric relations among the products become amenable to experimental test, and ratios of elementary rate constants and changes of some radical concentrations have been calculated.
Part I of this series ${ }^{1}$ dealt with the thermal decomposition of ethylal, dimethyl acetal, and diethyl acetal in a static system. The present paper extends the investigation to the simplest acetal, namely, methylal. With it a more thorough study of the decomposition mechanism has been undertaken by applying the steady-state approximation.

## Experimental and Results

The experimental technique was as described in Part I. Methylal was a purum grade " Fluka A.G." chemical.

Influence of the Surface.-Experiments were made in two vessels of the same size and shape, one empty and the other filled with silica powder, which varies the surface : volume ratio $\sim 500$-fold.

Plots of pressure increase against time for the first experiments in the filled vessel showed a shift towards greater values of $\Delta p$, compared with those obtained with the empty vessel. However, after several runs the shift decreased and finally the curves were superimposable. It seems that the thermal decomposition of methylal can be affected by the surface of the reaction vessel, but that this influence is probably relevant to a non-seasoned surface. These results suggest that in a seasoned vessel measurements refer to the true homogeneous decomposition. Other results (below) were obtained in seasoned vessels.

Table 1.
Rates of decomposition of methylal.

| $520^{\circ}$ | $p_{0}$ | 76 | 114 | 148 | 200 | 251 | 255 | 296 | 329 | 338 |  |
| :--- | :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :--- |
|  | Rate | 28 | 52 | 71 | 109 | 144 | 148 | 194 | 192 | 212 |  |
| $510^{\circ}$ | $p_{0}$ | 65 | 83 | 140 | 209 | 262 | 327 | 368 |  |  |  |
|  | Rate | 18 | 40 | 45 | 83 | 104 | 139 | 152 |  |  |  |
| $500^{\circ}$ | $p_{0}$ | 47 | 99 | 117 | 166 | 210 | 250 | 321 | 357 | 443 |  |
|  | Rate | 9 | 17 | 24 | 41 | 51 | 71 | 97 | 105 | 152 |  |
| $492^{\circ}$ | $p_{0}$ | 99 | 116 | 119 | 170 | 196 | 252 | 261 | 330 | 352 | 446 |
|  | Rate | 11 | 17 | $17 \cdot 5$ | 28 | $33 \cdot 5$ | 48 | 52 | 69 | 76 | 106 |
| $483^{\circ}$ | $p_{0}$ | 72 | 126 | 175 | 211 | 247 | 261 | 302 | 373 | 436 |  |
|  | Rate | $5 \cdot 5$ | $12 \cdot 5$ | 20 | 26 | 30 | 35 | 41 | $52 \cdot 5$ | 64 |  |
| $472^{\circ}$ | $p_{0}$ | 112 | 165 | 207 | 248 | 293 | 325 | 359 | 432 |  |  |
|  | Rate | $6 \cdot 5$ | 11 | 16 | 20 | 22 | $28 \cdot 5$ | $31 \cdot 5$ | $41 \cdot 5$ |  |  |

Pressures are in terms of mm . of Hg . Rates are recorded as mm . of $\mathrm{Hg} / \mathrm{min}$.
Change of Pressure.-Methylal was studied in the range $472-520^{\circ}$ and $50-450 \mathrm{~mm}$. (Fig. 1). Short induction periods were observed at the lower temperatures.

The kinetic constants have been determined from plots of pressure increase against time because it was found that for at least the first $70 \%$ of the reaction, the amount of methylal used is proportional to $\Delta p$ (Fig. 2). It was also shown that plots of the amounts of the products (carbon monoxide, methane, and hydrogen) against $\Delta p$ all yield straight lines that pass through the origin, and so the pressure increase becomes a measure of the rate of consumption of methylal.

The variation of the rate of the reaction with initial methylal pressure $\left(p_{0}\right)$ is recorded for

[^0]various temperatures in Table 1. Plots of the rate of the reaction against $p_{0}$ are curves for initial pressures up to about 150 mm . At the higher pressures it might be expected that the reaction should follow a first-order law, but experiments at still higher pressures might prove that the plot is actually a curve over the whole range.

An activation energy of $45 \mathrm{kcal} . /$ mole has been calculated by the method of least squares from the Arrhenius equation by using the values in Table 1.

Analysis of Products.-The analytical work was done (a) on two different fractions from one sample and (b) also by analysis of a second sample that had been similarly pyrolysed but not fractionated.


Fig. 1. Decomposition of methylal at (I) $472^{\circ}$, (II) $483^{\circ}$, (III) $492^{\circ}$, (IV) $500^{\circ}$, (V) $510^{\circ}$, and (VI) $520^{\circ}$. Initial pressures were 250 mm .


Fig. 2. Plot of pressure increase against decomposition at (O) $520^{\circ}$, ( $) 492^{\circ}$, and (○) $459^{\circ}$.

The calculated values of the amounts of methylal obtained from the amounts of the products are a little higher than those obtained by direct analysis of methylal, probably owing to absorption in the tap grease.

The following compounds have been identified by infrared spectrometry in the reaction mixture: carbon monoxide, carbon dioxide, methane, methyl alcohol, methyl formate, and undecomposed methylal. Hydrogen was determined by difference and by material balances.

Table 2.
Product analyses (methylal, $p_{0} 150 \mathrm{~mm}$.) (pressures in mm . of Hg ).

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline \multicolumn{2}{|l|}{\begin{tabular}{l}
Reaction \\
Temp. time (min.)
\end{tabular}} \& \(\mathrm{CH}_{4}\) \& \(\mathrm{H} \cdot \mathrm{CO}_{2} \mathrm{Me}\) \& MeOH \& CO \& \(\mathrm{H}_{2}\) \& \(\mathrm{CO}_{2}\) \& \multirow[t]{2}{*}{\[
\underset{121}{\mathrm{CH}_{2}(\mathrm{OMe})_{2}}
\]} \& \(\Sigma p\) \& Press. in vessel \\
\hline \multirow[t]{6}{*}{459

492} \& 8 \& $24 \cdot 5$ \& 15 \& - \& 19 \& 14 \& , \& \& 193 \& 190 <br>
\hline \& 15 \& 44 \& 22 \& - \& 33 \& 28 \& - \& 95 \& 222 \& $223 \cdot 5$ <br>
\hline \& 30 \& 72 \& 32 \& 7 \& 55 \& 40 \& - \& $75 \cdot 5$ \& 281.5 \& 286 <br>
\hline \& 45 \& 81.5 \& 37 \& 7.5 \& 62 \& 59 \& - \& 64 \& 311 \& 317 <br>
\hline \& 4 \& $43 \cdot 5$ \& 23 \& 5 \& 29 \& 44 \& - \& 94 \& 238.5 \& 240 <br>
\hline \& 6 \& 59 \& 33.5 \& $5 \cdot 5$ \& 78 \& 38 \& -- \& 81 \& 295 \& 287 <br>
\hline \multirow{14}{*}{520} \& 8 \& 61 \& 33 \& 5 \& 72 \& 71 \& -- \& 62 \& 304 \& 300 <br>
\hline \& 10 \& 97 \& 32 \& 5 \& 77.5 \& 50 \& - \& 62 \& 323 \& 323 <br>
\hline \& 12 \& 82 \& $43 \cdot 5$ \& 6 \& 85 \& $75 \cdot 5$ \& -- \& 56 \& 348 \& 346 <br>
\hline \& 12 \& $75 \cdot 5$ \& 38 \& $3 \cdot 5$ \& 81 \& 102 \& - \& 53 \& 353 \& 350 <br>
\hline \& 15 \& 83 \& 39.5 \& 4 \& 104 \& 92 \& 3 \& 50 \& $375 \cdot 5$ \& 358 <br>
\hline \& 20 \& 98 \& 39.5 \& 7 \& 104 \& 104 \& 3 \& 40 \& 395.5 \& 392 <br>
\hline \& 180 \& 111 \& 25 \& 9 \& 140 \& 158 \& $7 \cdot 5$ \& 25 \& $475 \cdot 5$ \& 464 <br>
\hline \& 2 \& 66.5 \& 30 \& 7.5 \& 59.5 \& 51.5 \& - \& 70 \& 285 \& 284 <br>
\hline \& 4 \& 106 \& 36 \& 7 \& 93 \& 52 \& 3 \& 49.5 \& 346.5 \& 344 <br>
\hline \& 6 \& 104 \& 37 \& 7.5 \& 100 \& 60.5 \& 9 \& 39.5 \& 357.5 \& 356 <br>
\hline \& 8 \& 113 \& $35 \cdot 5$ \& 7 \& 107 \& 91.5 \& 8 \& 31 \& 393 \& 393 <br>
\hline \& 10 \& 124 \& 36 \& 19 \& 104 \& 111 \& 12 \& 26 \& 432 \& 414 <br>
\hline \& 12 \& 122 \& 34 \& 10.5 \& 114 \& 117 \& 12 \& 29 \& 438.5 \& 421 <br>
\hline \& 18 \& 120 \& 31 \& 10 \& 115 \& 114 \& 18 \& 26 \& 434 \& 416 <br>
\hline
\end{tabular}

Quantitative analyses have been made for reactions at different temperatures (459, $492^{\circ}$, and $520^{\circ}$ ) and after different times. The results are recorded in Table 2.

Influence of Inhibitors.-Small amounts of nitric oxide $(<1 \%)$ inhibit the thermal decomposition of methylal. This may be considered as full inhibition because greater amounts do not decrease the rate further. Here also, as with the other acetals previously studied, inhibition is transitory.

Fig. 3. Inhibition of decomposition of methylal ( $p_{0} 150 \mathrm{~mm}$.) at $520^{\circ}$ by the following propene pressures: (I) 0 , (II) 2, (III) 4, (IV) 12 , (V) 20 , (VI) 30, (VII) 46, (VIII) 100, and (IX) 151 mm .


The reaction is inhibited also by propene but it is necessary to add nearly 150 mm . of propene to obtain the same reduction in the initial rate as with only 0.5 mm . of nitric oxide; however, the inhibition is not transitory with propene (Fig. 3).

## Discussion

Stoicheiometry.-The following partial equations (written only from the point of view of stoicheiometry) seem to explain formation of all the products:
(a) $\mathrm{CH}_{2}(\mathrm{OMe})_{2} \longrightarrow \mathrm{CH}_{4}+\mathrm{H} \cdot \mathrm{CO}_{2} \mathrm{Me}$
(b) $\mathrm{CH}_{2}(\mathrm{OMe})_{2} \longrightarrow 2 \mathrm{H}_{2}+2 \mathrm{CO}+\mathrm{CH}_{4}$
(c) $\mathrm{CH}_{2}(\mathrm{OMe})_{2} \longrightarrow \mathrm{MeOH}+\mathrm{CH}_{4}+\mathrm{CO}$
(d) $\mathrm{H} \cdot \mathrm{CO}_{2} \mathrm{Me} \longrightarrow \mathrm{CH}_{4}+\mathrm{CO}_{2}$
(e) $\mathrm{H} \cdot \mathrm{CO}_{2} \mathrm{Me} \longrightarrow \mathrm{CO}+\mathrm{MeOH}$
(f) $\mathrm{MeOH} \longrightarrow 2 \mathrm{H}_{2}+\mathrm{CO}$

Of these, the first two are the most important, and the last three probably occur only at the higher temperatures, where secondary decomposition of the products commences. The form of the curves at $520^{\circ}$ suggests that methyl formate decomposes.

At $459^{\circ}$, secondary decomposition, if present, must be unimportant and so the stoicheiometry of the reaction may be established at this temperature:

$$
26 \mathrm{CH}_{2}(\mathrm{OMe})_{2} \longrightarrow 26 \mathrm{CH}_{4}+13 \mathrm{H} \cdot \mathrm{CO}_{2} \mathrm{Me}+3 \mathrm{MeOH}+20 \mathrm{H}_{2}+23 \mathrm{CO}
$$

which again implies that reactions (a) and (b) account for most of the products.
The Chain Sequence.-The kinetic constants, analyses of products, and action of inhibitors may be explained by a chain mechanism as follows:
(a) Initiation.
(I) $\mathrm{CH}_{2}(\mathrm{OMe})_{2} \longrightarrow \mathrm{MeO} \cdot \mathrm{CH}_{2} \cdot \mathrm{O} \cdot+\mathrm{Me} \cdot$
(2) $\mathrm{MeO} \cdot \mathrm{CH}_{2} \cdot \mathrm{O} \longrightarrow \mathrm{H} \cdot+\mathrm{H} \cdot \mathrm{CO}_{2} \mathrm{Me}$

The initial splitting could be also into a methoxyl radical and the remaining radical, but this would not greatly affect the whole chain process.
(b) Propagation. It seems obvious that in propagation attack is on one hydrogen atom of the $\mathrm{CH}_{2}$ group of methylal. In the following, R denotes the radical $(\mathrm{MeO})_{2} \mathrm{CH} \cdot$

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We then propose the steps:
(3) $\mathrm{CH}_{2}(\mathrm{OMe})_{2}+\mathrm{H} \longrightarrow \mathrm{H}_{2}+\mathrm{R}$.
(4) R . $\longrightarrow \mathrm{H} \cdot \mathrm{CO}_{2} \mathrm{Me}+\mathrm{Me}$.
(5) $\mathrm{CH}_{2}(\mathrm{OMe})_{2}+\mathrm{Me} \longrightarrow \mathrm{CH}_{4}+\mathrm{R}$.
(6) $\mathrm{R} \cdot \quad \longrightarrow \mathrm{MeO} \cdot+\mathrm{MeO} \cdot \mathrm{CH}^{-}$
(7) $\mathrm{CH}_{2}(\mathrm{OMe})_{2}+\mathrm{MeO} \longrightarrow \mathrm{MeOH}+\mathrm{R}$.
(8) $\mathrm{MeO} \cdot \longrightarrow \mathrm{H} \cdot+\mathrm{CO}+\mathrm{H}_{2}$

Acetaldehyde has not been detected among the products over the range studied; consequently, the rearrangement $\mathrm{CH}_{2}(\mathrm{OMe})_{2} \longrightarrow \mathrm{MeOH}+\mathrm{Me} \cdot \mathrm{CHO}$ seems to be excluded, and this is the reason why methoxyl radicals should be present in order to account for the methyl alcohol formed.

The small quantity of carbon dioxide formed could be explained partially by the reaction:

though it is more likely to arise from the secondary decomposition of methyl formate that occurs at the higher temperatures studied.
(c) Termination.


The reaction $2 \mathrm{Me} \cdot \longrightarrow \mathrm{C}_{2} \mathrm{H}_{6}$ has not been considered because ethane is not produced. Reactions of a radical with a different one have also not been considered, as no other products have been detected in the mixtures.

Steady-state Equations.-The steady-state approximation requires that

$$
\begin{gather*}
k_{3} \mathrm{MH}-\left(k_{4}+k_{6}\right) \mathrm{R}+k_{5} \mathrm{MA}+k_{7} \mathrm{MB}-k_{11} \mathrm{RH}=0 ;  \tag{i}\\
k_{1} \mathrm{M}+k_{4} \mathrm{R}-k_{5} \mathrm{MA}-k_{12} \mathrm{HA}=0 ;  \tag{ii}\\
k_{1} \mathrm{M}-k_{3} \mathrm{MH}+k_{8} \mathrm{~B}-k_{10} \mathrm{H}^{2}-k_{11} \mathrm{RH}-k_{12} \mathrm{HA}-k_{13} \mathrm{HB}=0 ;  \tag{iii}\\
k_{6} \mathrm{R}-\mathrm{B}\left(k_{7} \mathrm{M}+k_{8}+k_{13} \mathrm{H}\right)=0 \tag{iv}
\end{gather*}
$$

where $\mathrm{M}, \mathrm{H}, \mathrm{A}, \mathrm{B}$, and R denote the concentrations of methylal, hydrogen atoms, and methyl, methoxyl, and R radicals, respectively.

Two independent expressions for $\mathrm{R} / \mathrm{M}$ may be thence derived:

$$
\begin{equation*}
\frac{\mathrm{R}}{\mathrm{M}}=\frac{\mathrm{H}}{2 k_{8} k_{8}}\left(2 k_{3}+k_{10} \frac{\mathrm{H}}{\overline{\mathrm{M}}}\right)\left(k_{7} \mathrm{M}+k_{13} \mathrm{H}+k_{8}\right) \tag{v}
\end{equation*}
$$

and

$$
\begin{equation*}
\stackrel{\mathrm{R}}{\overline{\mathrm{M}}}\left(\frac{k_{4} k_{12}}{k_{5} \mathrm{M}+k_{12} \mathrm{H}}+\frac{k_{6} k_{13}}{k_{7} \mathrm{M}+k_{13} \mathrm{H}+k_{8}}+k_{11}\right)=\frac{k_{1} k_{5} \mathrm{M}}{\overline{\mathrm{H}}\left(k_{5} \mathrm{M}+k_{12} \overline{\mathrm{H}}\right)}-\frac{k_{10}}{2} \cdot \frac{\mathrm{H}}{\overline{\mathrm{M}}} . \tag{vi}
\end{equation*}
$$

Substitution of the $R / M$ value from (v) into (vi) gives the general expression that relates H and M ; this is a fifth-order equation which cannot be solved for H . However, as will be shown, some chain steps offer a minor contribution to the mechanism and may be neglected, thus simplifying the treatment.

The rate of consumption of methylal may be expressed by

$$
\begin{equation*}
-\mathrm{dM} / \mathrm{d} t=k_{1} \mathrm{M}+k_{3} \mathrm{MH}+k_{5} \mathrm{MA}+k_{7} \mathrm{MB}-k_{11} \mathrm{RH} \tag{vii}
\end{equation*}
$$

and subtraction of (i) from (vii) gives the simpler expression

$$
\begin{equation*}
-\frac{1}{\mathrm{M}} \cdot \frac{\mathrm{dM}}{\mathrm{~d} t}=k_{1}+\left(k_{4}+k_{6}\right) \frac{\mathrm{R}}{\mathrm{M}} \tag{viii}
\end{equation*}
$$

If methylal were consumed according to a first-order law, R/M should be a constant in (viii). Consideration of equations (v) and (vi) shows that this condition would probably be fulfilled if $H, H / M$, and $M$ were constant. But, as the value of $M$ changes greatly in the course of the reaction, it is not possible to accept that $H$ and $H / M$ remain simultaneously constant. Consequently, a first-order law would probably require that steps (7), (10), and (12) were negligible.

The experimental behaviour is considered to be almost that required by a first-order law, but close examination shows some deviations. This raises the suspicion that among steps (7), (10), and (12) there is one or more which participate in the proposed mechanism.

Let us consider the building-up rates of the products if steps (10) and (12) are ignored:

$$
\begin{gather*}
\mathrm{d}\left[\mathrm{CH}_{4}\right] / \mathrm{d} t=-\mathrm{dM} / \mathrm{d} t=k_{1} \mathrm{M}+\left(k_{4}+k_{6}\right) \mathrm{R} ;  \tag{ix}\\
\mathrm{d}[\mathrm{CO}] / \mathrm{d} t=k_{6} \mathrm{R}\left\{\mathbf{1}+k_{8} /\left(k_{7} \mathrm{M}+k_{8}+k_{13} \mathrm{H}\right)\right\} ;  \tag{x}\\
\mathrm{d}\left[\mathrm{H} \cdot \mathrm{CO}_{2} \mathrm{Me}\right] / \mathrm{d} t=k_{1} \mathrm{M}+k_{4} \mathrm{R} ;  \tag{xi}\\
\mathrm{d}\left[\mathrm{H}_{2}\right] / \mathrm{d} t=k_{3} \mathrm{MH}+k_{6} k_{8} \mathrm{R} /\left(k_{7} \mathrm{M}+k_{8}+k_{13} \mathrm{H}\right) ;  \tag{xii}\\
\mathrm{d}[\mathrm{MeOH}] / \mathrm{d} t=k_{6} \mathrm{R}\left(k_{13} \mathrm{H}+k_{7} \mathrm{M}\right) /\left(k_{7} \mathrm{M}+k_{8}+k_{13} \mathrm{H}\right) . \tag{xiii}
\end{gather*}
$$

If step (7) were also neglected (i.e., $k_{7}=0$ ), the following would be obtained from the preceding equations together with (vi):

$$
\begin{equation*}
\frac{k_{11}}{k_{3} k_{6}}=\frac{4 k_{1}-2 V_{\mathrm{MeOH}}}{\left(\overline{\left.V_{\mathrm{CO}}+V_{\mathrm{MeOH}}\right)\left(V_{\mathrm{CO}}-V_{\mathrm{MeOH}}\right.}\right)}, \tag{xiv}
\end{equation*}
$$

where $V$ denotes the corresponding rates divided by M .
The condition

$$
\begin{equation*}
2 k_{1} \mathrm{M}>\mathrm{d}[\mathrm{MeOH}] / \mathrm{d} t \tag{xv}
\end{equation*}
$$

is immediately derivable from (xiv) but is unacceptable if long chains are assumed because $k_{1} \mathrm{M}$ is the chain-initiation rate. This result implies that the derivation of (xiv) fails because it does not account for the methyl alcohol found experimentally; in other words, step (7) cannot be neglected in the proposed mechanism. Only $k_{10}$ and $k_{12}$ may be equated to zero, which is a reasonable conclusion if the need of a third body in the corresponding steps is taken into account.

Consequently, in the following treatment the chain sequence proposed will be considered with only the exception of steps (10) and (12).

The Order at Zero Reaction Time.-If the theory is to be acceptable, expressions should be derivable for the experimental order.

By solving for M in the general equation that results from (v) and (vi), we obtain

$$
\begin{equation*}
\mathrm{M}=\frac{k_{1} k_{6} k_{8}}{k_{3} k_{7} k_{11}} \cdot \frac{1}{\mathrm{H}_{2}}-\frac{k_{13}}{k_{7}} \cdot \mathrm{H}-\frac{k_{6} k_{13}+k_{8} k_{11}}{k_{7} k_{11}}, \tag{xvi}
\end{equation*}
$$

which is still much too complicated for direct solution.
According to equation (xvi), the value of H should increase as M diminishes and the presence of the term $k_{7} \mathrm{M}$ lowers the hydrogen-atom concentration in the reaction mixture.

If an almost zero reaction time were considered, where the steady-state approximation might already apply, then $\mathrm{M} \approx \mathrm{M}_{0}$ and the hydrogen-atom concentration would attain its lower value $\mathrm{H}_{0}$.

From equations (vi), (ix), and (xvi) the following is derived at $t=0$ :
where

$$
\begin{align*}
-(\mathrm{d} \mathrm{M} / \mathrm{d} t)_{0} & =\mathrm{M}_{0}\left\{k_{1}+P[\sqrt{ }(\mathbf{1}+x)-\mathbf{1} / \sqrt{ }(\mathbf{1}+x)]\right\} \\
& =k_{1} \mathrm{M}_{0}+\mathrm{M}_{0} P x / \sqrt{ }(\mathbf{1}+x) \tag{xvii}
\end{align*}
$$

$$
\begin{equation*}
x=\frac{k_{7} k_{11}}{k_{6} k_{13}} \cdot \mathrm{M}_{0}+\frac{k_{11}\left(k_{8}+k_{13} \mathrm{H}_{0}\right)}{k_{6} k_{13}} \tag{xviii}
\end{equation*}
$$

and

$$
\begin{equation*}
P=\frac{k_{4}+k_{6}}{k_{11}} \sqrt{\frac{k_{1} k_{3} k_{13}}{k_{8}} .} \tag{xix}
\end{equation*}
$$

The $k_{1} \mathrm{M}_{0}$ term may be neglected in (xvii) if, as has been supposed, steady-state conditions hold. Though not exact, this is a fair assumption provided a comparatively high temperature is chosen where no induction period is found in the $\Delta p$-time curves. So, from inspection of equation (xvii), a reaction order not far from 1.5 would be expected. This conclusion has been checked experimentally in the $472-520^{\circ}$ range in Fig. 4 where the series of parallel straight lines corresponds to a 1.3 order.


Fig. 4. Plots showing a $1 \cdot 3$ order at
(I) $422^{\circ}$, (II) $483^{\circ}$, (III) $492^{\circ}$, (IV) $500^{\circ}$, (V) $510^{\circ}$, and (VI) $520^{\circ}$.

Moreover, it can be shown that the experimental results are in accordance with the theoretical implications of eqn. (xvii), by fitting the parameters involved.

As will be seen below, there are reasons to believe that $k_{13} \mathrm{H}_{0}$ is rather small with respect to $k_{8}$. Consequently, $x$ might be considered as a linear function of $\mathrm{M}_{0}$ :

$$
\begin{equation*}
x=a \mathrm{M}_{0}+b \tag{xx}
\end{equation*}
$$

Plotting the experimental values of $-\frac{1}{\mathrm{M}}\left(\frac{\mathrm{dM}}{\mathrm{d} t}\right)_{0}$ at $492^{\circ}$ against $\mathrm{M}_{0}$ enables values of $a, b$, and $P$ to be found that lead to superimposition of the experimental function on the theoretical equation (xvii). Table 3 shows the values used in the calculation. The following values then lead (Fig. 5) to a satisfactory fit:

$$
\begin{gathered}
a=k_{7} k_{11} / k_{6} k_{13} \approx 0.002 \mathrm{~mm} .^{-1} ; b / a=\left(k_{8}+k_{13} \mathrm{H}_{0}\right) k_{7}=168 \mathrm{~mm} \\
P=0.15 \mathrm{~min} . .^{-1}
\end{gathered}
$$

Table 3.
Values at $492^{\circ}$.

| $-\frac{1}{M_{0}}\left(\frac{\mathrm{dM}}{\mathrm{d} t}\right)_{0}\left(\min .^{-1}\right) \ldots$ | 0.0583 | 0.0655 | 0.0783 | 0.0867 | 0.0950 | 0.1016 | 0.1071 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{M}_{0}(\mathrm{~mm})$. | $\ldots \ldots \ldots \ldots .$. | 60 | 100 | 150 | 200 | 250 | 300 | 350 |

The Reaction Order.-From expressions (v) and (ix) the following may be derived:
where

$$
\begin{equation*}
-\mathrm{d} \ln \mathrm{M}=A_{0} \mathrm{~d} t+A_{1} \mathrm{M} \mathrm{~d} t \tag{xxi}
\end{equation*}
$$

and

$$
\begin{equation*}
A_{0}=k_{1}+\left(k_{4}+k_{6}\right) k_{3} \mathrm{H}\left(k_{13} \mathrm{H}+k_{8}\right) / k_{6} k_{8} \tag{xxii}
\end{equation*}
$$

The experimental results seemed explicable if a first-order law held to $>50 \%$ conversion, but this is not the only explanation. Equation (xxi) does not contradict these results provided $A_{0}+A_{1} \mathrm{M}$ remains almost constant throughout the reaction. In that case, a plot of $\ln \mathrm{M}$ against time would yield an approximately straight line and the apparent order would be unity. However, if longer reaction times are considered, some discrepancies from order one are to be expected from equation (xxi). In fact, in the plot


Fig. 5. Coincidence of experimental points and calculation.


Fig. 6. Plots for decomposition of methylal ( $p_{0} 150 \mathrm{~mm}$.) at $497^{\circ}$ : (I) $p_{\infty} 300 \mathrm{~mm}$.; (II) $p_{\infty} 310 \mathrm{~mm}$.
of $\log \left(p_{\infty}-p\right)$ against $t$ (which is equivalent to the plot of $\ln \mathrm{M}$ against time) a straight line is no longer obtained (Fig. 6). This result is in agreement with equation (xxi) according to which an upward curvature at the shorter times is to be expected. Unfortunately there is no fixed criterion for the choice of $p_{\infty}$, so the exact position of the straight line is ignored and the parameters of equation (xxi) cannot be calculated.

It should be emphasised that it is the presence of the $k_{7} \mathrm{M}$ term and, in consequence, the influence of step (7) on the mechanism which are greater than casual inspection indicates and are decisive for the curvature. If very long times are considered, the curves are seen to be sigmoid, the downward curvature being produced by secondary decomposition of the products or, more probably, by the influence of the $p_{\infty}$ selected.

Stoicheiometric Relations.-Several relations among the formation rates of the products may be derived from equations (ix)-(xiii). The rates may be replaced by concentrations because the curves so obtained are similar in shape and could be superimposed on the rate curves by changing the scales (provided high temperatures are avoided where secondary decompositions intervene).

From equation (ix) the following relation is immediately obtainable:

$$
\begin{equation*}
\left[\mathrm{CH}_{4}\right]=\mathrm{M}_{0}-\mathrm{M} \tag{xxiv}
\end{equation*}
$$

From (ix-xi) and (xiii) we obtain

$$
\begin{equation*}
[\mathrm{CO}]+[\mathrm{MeOH}]+2\left[\mathrm{H} \cdot \mathrm{CO}_{2} \mathrm{Me}\right]=2\left[\mathrm{CH}_{4}\right] \tag{xxv}
\end{equation*}
$$

and from (ix-xiii) and (v)

$$
\begin{equation*}
[\mathrm{CO}]=[\mathrm{MeOH}]+\left[\mathrm{H}_{2}\right] \tag{xxvi}
\end{equation*}
$$

The results from relations (xxiv-xxvi) are reported in Tables 4 and 5. Calculations have not been made for higher temperatures because of secondary decomposition of methyl formate and, perhaps, of methyl alcohol.

Table 4.
Results (pressures in min.) of calculations $\left[p_{0}\right.$ for $\mathrm{CH}_{2}(\mathrm{OMe})_{2},=150 \mathrm{~mm}$.].

| Te | $459{ }^{\circ}$ |  |  |  |  | $\underbrace{495}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Time (min.) ........ | 8 | 16 | 24 | 32 | 40 | 4 | 8 | 12 | 16 | 20 |
| $\left[\mathrm{C}_{3} \mathrm{H}_{8} \mathrm{O}_{2}\right] \ldots \ldots \ldots \ldots .$. | 120 | 100 | 85 | 75 | 70 | 105 | 73 | 55 | 44 | 40 |
| $\left[\mathrm{CH}_{4}\right]^{2} \ldots \ldots . . . . . . . .$. | 27 | 48 | 62 | 72 | 78 | 43 | 71 | 86 | 94 | 100 |
| $\left[\mathrm{C}_{3} \mathrm{H}_{8} \mathrm{O}_{2}\right]+\left[\mathrm{CH}_{4}\right] \ldots$ | 147 | 148 | 147 | 147 | 148 | 148 | 144 | 141 | 138 | 140 |

Table 5.
Results (pressures in mm.) of calculations $\left[p_{0}\right.$ for $\mathrm{CH}_{2}(\mathrm{OMe})_{2}=150 \mathrm{~mm}$.].

| Temp. | $459^{\circ}$ |  |  | $492^{\circ}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Time (min.) ................ | 4 | 16 | 32 | 4 | 8 | 12 |
| [CO].. | 11 | 35 | 56 | 43 | 70 | 88 |
| [ MeOH ] | 2 | 4 | 6.5 | 5 | 6 | 7 |
| [ $\mathrm{H} \cdot \mathrm{CO}_{2} \mathrm{Me}$ ] | 7 | 23.5 | 68 | 20 | 33 | 39 |
| $[\mathrm{CO}]+[\mathrm{MeOH}]+2\left[\mathrm{H} \cdot \mathrm{CO}_{2} \mathrm{Me}\right]$ | 27 | 86 | $130 \cdot 5$ | 88 | 142 | 173 |
| $2\left[\mathrm{CH}_{4}\right] \ldots . . . . . . .$. | 28 | 92 | 142 | 86 | 142 | 172 |
| $[\mathrm{MeOH}]+\left[\mathrm{H}_{2}\right]$ | 10 | 33 | $55 \cdot 5$ | 43 | 71 | 87 |

Ratios among the Rate Constants.-From expressions (ix) and (xi) the following may be derived, where $k_{1}$ is very small and may be neglected:

$$
\begin{equation*}
\frac{k_{6}}{k_{4}}=\frac{V_{\mathrm{CH}_{4}}-k_{1}}{V_{\mathrm{H} \cdot \mathrm{CO}_{2} \mathrm{Me}_{\mathrm{e}}}-k_{1}}-1 \approx \frac{V_{\mathrm{CH}_{4}}}{V_{\mathrm{H} \cdot \mathrm{CO}_{\mathbf{2}} \mathrm{Me}}}-1 . \tag{xxvii}
\end{equation*}
$$

(The $V$ 's, as previously, denote the corresponding rates divided by M.)
Equations (ix-xiii) and use of the $\mathrm{R} / \mathrm{M}$ values from equation (v) lead to

$$
\begin{equation*}
\frac{k_{7}}{k_{8}}+\frac{k_{13}}{k_{8} k_{3}} \cdot \frac{V_{\mathrm{H}_{3}}}{2 \mathrm{M}}=\frac{2 V_{\mathrm{MeOH}}}{\mathrm{M} V_{\mathrm{H}}} \tag{xxviii}
\end{equation*}
$$

If equations (vi), (ix-xiii), and (xxviii) are used, we obtain

$$
\begin{equation*}
\frac{k_{7}}{k_{8}}+\frac{2 k_{1}}{\overline{\mathrm{M}} V_{\mathrm{H}_{2}}}-\frac{k_{11}}{2 k_{3} k_{6} \mathrm{M}}\left(V_{\mathrm{CO}}+V_{\mathrm{MeOH}}\right)=\frac{2 V_{\mathrm{MeOH}}}{\mathrm{M} V_{\mathrm{H}_{2}}} . \tag{xxix}
\end{equation*}
$$

Relations (xxvii-xxix) constitute a set of independent equations and, although others may be obtained, they are derivable from them.

By using the experimental values of the appearance rates of the products from Table 6 it is possible to calculate the ratios among the rate constants in the preceding equations.

Table 6.
Rates (mm./min.) of formation of products from methylal ( $p_{0} \mathbf{1 5 0} \mathbf{~ m m}$.).

| Temp. | $\begin{aligned} & \text { Time } \\ & \text { (min.) } \end{aligned}$ | $\mathrm{d}\left[\mathrm{H}_{2}\right] / \mathrm{d} t$ | $\mathrm{d}[\mathrm{CO}] / \mathrm{d} t$ | $\mathrm{d}\left[\mathrm{CH}_{4}\right] / \mathrm{d} t$ | $\mathrm{d}\left[\mathrm{H} \cdot \mathrm{CO}_{3} \mathrm{Me}\right] / \mathrm{d} t$ | $\mathrm{d}[\mathrm{MeOH}] / \mathrm{d} t$ | $\begin{gathered} \mathrm{M} \\ (\mathrm{~mm} .) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $459{ }^{\circ}$ | 4 | 2 | $2 \cdot 5$ | $3 \cdot 45$ | $1 \cdot 6$ | 0.32 | 135 |
|  | 16 | 1.45 | 1.7 | $2 \cdot 17$ | 1.05 | $0 \cdot 2$ | 105 |
|  | 32 | $0 \cdot 88$ | $0 \cdot 95$ | 1 | 0.5 | $0 \cdot 08$ | 71 |
| 492 | 4 | $8 \cdot 2$ | 8 | $8 \cdot 3$ | $4 \cdot 3$ | $1 \cdot 1$ | 105 |
|  | 8 | $5 \cdot 9$ | $5 \cdot 3$ | $5 \cdot 5$ | 2 | $0 \cdot 55$ | 73 |
|  | 12 | $4 \cdot 1$ | $3 \cdot 5$ | 3 |  | $0 \cdot 3$ | 55 |

The ratio $k_{6}: k_{4}$ obtained in this way from equation (xxvii) is about unity at $459^{\circ}$. The results at $492^{\circ}$ are a little doubtful because some methyl formate is probably decomposed, but the ratio is still of the same order of magnitude.

By means of equation (xxviii) the values of $k_{7} / k_{8}$ and of $k_{13} /\left(k_{8} k_{3}\right)$ are obtainable in
principle if the experimental values at two different times from Table 6 are substituted and the resulting system is solved for the rate constant ratios.

However, in this way the experimental errors lead to uncertainty and only the orders of magnitude are real. Nevertheless, the following inequalities may be derived from equations (xxviii) and (xxix):

$$
\begin{gather*}
\frac{2 k_{1}}{\mathrm{~d}\left[\mathrm{H}_{2}\right] / \mathrm{d} t}+\frac{k_{7}}{k_{8}}>\frac{2}{\overline{\mathrm{M}}} \frac{\mathrm{~d}[\mathrm{MeOH}] / \mathrm{d} t}{\mathrm{~d}\left[\mathrm{H}_{2}\right] / \mathrm{d} t}>\frac{k_{7}}{k_{8}} \\
\frac{k_{7}}{k_{8}} \approx \frac{2}{\mathrm{M}} \cdot \frac{\mathrm{~d}[\mathrm{MeOH}] / \mathrm{d} t}{\mathrm{~d}\left[\mathrm{H}_{2}\right] / \mathrm{d} t}, \tag{xxx}
\end{gather*}
$$

which allows us to calculate the value $k_{7} / k_{8}$; it is $0.0025 \mathrm{~mm} .{ }^{-1}$ at $459^{\circ}$. The error incurred by neglecting the term $\frac{2 k_{1}}{\mathrm{~d}\left[\mathrm{H}_{2}\right] / \mathrm{d} t}$ would be in the third significant figure if $k_{1}=1.5 \times 10^{-5}$ $\mathrm{min} .^{-1}$, and in the second if $k_{1}=7 \times 10^{-5} \mathrm{~min} .^{-1}$.

Incidentally, being a different form of equation (xxviii), namely,

$$
\begin{equation*}
\frac{k_{7} \mathrm{M}}{k_{8}}+\frac{k_{13} \mathrm{H}}{k_{8}}=\frac{2 V_{\mathrm{MeOH}}}{V_{\mathrm{H}_{3}}} \tag{xxxi}
\end{equation*}
$$

and the value obtained for $k_{7} / k_{8}$ justifies considering ( $k_{13} \mathrm{H}_{0}+k_{8}$ ) as almost constant, as it is done in expressions (xviii) and ( xx ).

Variation of the Radical Concentrations.-Some equations may be derived from the preceding by rearrangement and substitution which allow us to calculate changes in radical concentrations.

From expressions (ix-xii) and (v) we derive
and

$$
\begin{gather*}
k_{3} \mathrm{H}=\frac{1}{2} V_{\mathrm{H}_{2}}  \tag{xxxii}\\
k_{6} \mathrm{R}=\left(V_{\mathrm{MeOH}}+\frac{1}{2} V_{\mathrm{H}_{3}}\right) \mathrm{M} \tag{xxxiii}
\end{gather*}
$$

where the value of the first term in each equation may be calculated at different reaction times (Table 7).

The hydrogen-atom concentration is roughly constant throughout the reaction but increases with temperature. The differences observed in Table 7 might be explained as due to the errors involved in the measurement of the concentration of the molecular hydrogen present in the reaction mixtures.

Table 7.
Concentrations of radicals.

|  | $459^{\circ}$ |  |  | $492^{\circ}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Time (min.) | 4 | 16 | 32 | 4 | 8 | 12 | 20 |
| Reaction (\%) | $7 \cdot 8$ | 27 | 45 | 30 | 50 | 63 | 73 |
| $k_{3} \mathrm{H}\left(\mathrm{min} .^{-1}\right)$. | $0 \cdot 0074$ | 0.0069 | $0 \cdot 0062$ | 0.039 | $0 \cdot 040$ | 0.039 |  |
| $k_{6} \mathrm{R}$ ( $\mathrm{min} .^{-1} \mathrm{~mm}$.) | $1 \cdot 9$ | $1 \cdot 1$ | 1 | 4 | $3 \cdot 5$ | 2 | $0 \cdot 8$ |

The concentration of the R radicals varies appreciably throughout an experiment and, as might be expected, is greater the higher the temperature. Table 7 shows that $k_{6} \mathrm{R} \gg$ $k_{3} \mathrm{H}$, although it is not possible to specify whether $k_{6}>k_{3}$ or $\mathrm{R}>\mathrm{H}$ or, perhaps, both.

The preceding mathematical treatment shows that the proposed chain sequence explains all the experimental facts concerning the decomposition of methylal, although it does not necessarily exclude other mechanisms. Several possibilities have intentionally

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been left out of account. One such is the equilibrium $\mathrm{Me} \cdot+\mathrm{H}_{2} \Longrightarrow \mathrm{H} \cdot+\mathrm{CH}_{4}$, which would not affect the results because certain steps in our chain sequence are equivalent to it. Another is initiation of the chain by the fission $\mathrm{CH}_{2}(\mathrm{OMe})_{2} \rightarrow \mathrm{MeO} \cdot+\mathrm{MeO}^{\cdot} \mathrm{CH}_{2} \cdot$ and participation of the latter radical in the propagation, the reason being that there is no need to postulate these radicals in order to explain the results.

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[^0]:    ${ }^{1}$ Part l, Molera, Centeno, and Orza, J., 1963, 2234.

